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MARK SCHEME

Maximum Mark: 100

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## Abbreviations

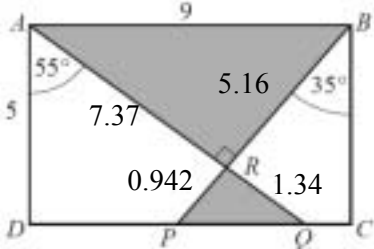
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
oe	or equivalent
SC	Special Case
nfw	not from wrong working
soi	seen or implied

Question	Answer	Marks	Partial Marks
1(a)(i)	503.5[0] <b>final answer</b>	<b>3</b>	<b>M2</b> for $12.50 \times 38 \times 1.06$ oe or $12.50 \times 38 \times 0.06$ oe or <b>M1</b> for $12.50 \times 38$ or $12.50 \times 1.06$ oe soi or $12.50 \times 0.06$ oe soi
1(a)(ii)	12	<b>2</b>	<b>M1</b> for $(525 - 462) \div 525$ oe After <b>M0</b> , <b>SC1</b> for answer 88
1(a)(iii)	2400 <b>nfw</b>	<b>2</b>	<b>M1</b> for $1.03x = 2472$ soi
1(b)	192	<b>3</b>	<b>M1</b> for $520 \times 0.74$ <b>M1</b> for $(\text{their } 384.8 - 260) \div 0.65$
2(a)	14.35 or 14.4	<b>3</b>	<b>B1</b> for use of correct midpoints soi  <b>M1</b> for $(2.5 \times 35 + 7.5 \times 42 + 15 \times 30 + 25 \times 28 + 40 \times 15) \div 150$
2(b)	Correct histogram with linear scale on frequency density axis	<b>3</b>	<b>B2</b> for all 5 bar heights correct with frequency density axis scaled OR <b>B1</b> for at least 3 correct heights drawn or 3 correct frequency densities calculated <b>B1</b> for 5 bars correct width and position
2(c)	18 to 20	<b>2</b>	<b>M1</b> for $(15 + 14) \div 150$
3(a)	040	<b>1</b>	
3(b)	$BC = \frac{\sqrt{25^2 + 38^2 - 2 \times 25 \times 38 \cos(360 - 220)}}{}$	<b>M2</b>	or <b>M1</b> for $25^2 + 38^2 - 2 \times 25 \times 38 \times \cos(360 - 220)$
	$BC = 59.36$ to $59.37$	<b>A1</b>	

Question	Answer	Marks	Partial Marks
3(c)	204.1 to 204.3[2...]	4	<b>B3</b> for 24.1 to 24.3[2...]  OR <b>M2</b> for $\sin B = \frac{38 \times \sin(360 - 220)}{59.4}$ or <b>M1</b> for $\frac{\sin B}{38} = \frac{\sin(360 - 220)}{59.4}$  and <b>M1</b> for 180 + <i>their B</i>
4(a)	$\frac{5}{9}$ oe	1	
4(b)(i)	$\frac{25}{81}$ oe	1	
4(b)(ii)	$\frac{40}{81}$ oe	2	<b>M1</b> for $\frac{\text{their } 5}{9} \times \frac{(9 - \text{their } 5)}{9}$ soi or  $\frac{\text{their } 5}{9} \times \frac{4}{9}$
4(c)	$\frac{4}{9}$ oe <b>nfww</b>	3	<b>M2</b> for $\frac{5}{9} \times \frac{4}{8} + \frac{4}{9} \times \frac{3}{8}$ or <b>M1</b> for $\frac{4}{9} \times \frac{3}{8}$ or $\frac{5}{9} \times \frac{4}{8}$
5(a)	-3 , 2 <b>nfww</b>	3	<b>M1</b> for $y^2 + 5y = 4y + 6$ <b>M1</b> for $(y + 3)(y - 2) [= 0]$
5(b)	$t = \frac{2p-1}{4+p}$ or $t = \frac{1-2p}{-4-p}$ <b>final answer</b>	3	<b>M1</b> for $p(2 - t) = 4t + 1$ or better <b>M1FT</b> for $2p - 1 = 4t + pt$  <b>M1FT</b> for completion to explicit formula for $t$  <b>Max 2 marks if final answer incorrect</b>
5(c)	$\frac{3x-2}{x+4}$ <b>final answer</b>	3	<b>B1</b> for $(3x - 2)(x - 4)$ seen <b>B1</b> for $(x + 4)(x - 4)$ seen
6(a)(i)	[ $\hat{ACB} = $ ] 38	1	
6(a)(ii)	[ $\hat{AEF} = $ ] 38, angles in same segment are equal	1	Strict <b>FT</b> <i>their</i> (i)
6(a)(iii)	[ $\hat{CDE} = $ ] 112	1	
6(a)(iv)	[ $\hat{BCD} = $ ] 106	2	<b>FT</b> 180 – <i>their CDE</i> + <i>their ACB</i> <b>M1</b> for $\hat{ACD} = 180 - \text{their } 112$ soi

Question	Answer	Marks	Partial Marks
6(b)	156	3	<b>B1</b> for sum of angles in pentagon = 540 soi <b>M1</b> for $8x + 124 = \text{their } 540$ oe
6(c)	105.5	2	<b>B1</b> for two of 65.5, 131.5 and 57.5 seen After <b>B0</b> , <b>SC1</b> for answer 108.5
7(a)(i)	$y = -2x + 5$ oe	2	<b>B1</b> for $y = -2x + c$ oe or for $y = mx + 5$ oe or <b>M1</b> for gradient = $\frac{5+3}{0-4}$ oe
7(a)(ii)	$y = -2x - 1$ oe <b>FT</b> their gradient from (a)(i)	2	<b>B1</b> for answer $y = \text{their } (-2)x + k$ , where $k \neq \text{their } 5$ or <b>M1</b> for $3 = \text{their } (-2) \times -2 + k$ oe
7(b)(i)	3.5	1	
7(b)(ii)	Correct smooth curve through 8 correct points	3	<b>B2FT</b> for 7 or 8 points correctly plotted or <b>B1FT</b> for 5 or 6 points correctly plotted
7(b)(iii)	Clear correct tangent drawn at (1, 1)	<b>M1</b>	
	-2.4 to -1.6	<b>A1</b>	
7(b)(iv)	0.6 to 0.8 and 4.2 to 4.4	2	<b>FT</b> reading from their graph at $y = 2$ <b>B1</b> for one correct or for $y = 2$ soi
8(a)	$[x^2 = ] 6^2 + 12^2$	<b>M1</b>	or $[x = ] \sqrt{6^2 + 12^2}$
	$[x = ] 13.41[6\dots]$ or 13.42	<b>A1</b>	
8(b)	478.7 to 479.4	3	<b>M1</b> for $\left[\frac{1}{2} \times\right] 4 \times \pi \times 6^2$ seen <b>M1</b> for $\pi \times 6 \times 13.4$ seen  After 0 scored, <b>SC1</b> for consistent use of $r = 3$ in formula for [hemi]sphere and cone
8(c)	904.7 to 905 <b>nfw</b>	3	<b>M1</b> for $\left[\frac{1}{2} \times\right] \frac{4}{3} \times \pi \times 6^3$ seen <b>M1</b> for $\frac{1}{3} \times \pi \times 6^2 \times 12$ seen  After 0 scored, <b>SC1</b> for consistent use of $r = 3$ in formula for [hemi]sphere and cone
8(d)(i)	4310 or <b>FT</b> $9 \times \text{their (b)}$	2	<b>M1</b> for $\left(\frac{6}{2}\right)^2$ soi
8(d)(ii)	113 or <b>FT</b> $\frac{1}{8} \times \text{their (c)}$	2	<b>M1</b> for $\left(\frac{1}{2}\right)^3$ soi

Question	Answer	Marks	Partial Marks
9(a)	7 cao	2	<b>M1</b> for $\frac{12}{3000} \times 1750$ oe
9(b)(i)	$\frac{2500}{x}$	1	
9(b)(ii)	$\frac{2500}{x} - \frac{2500}{x+20} = 15$	<b>M1</b>	Or equivalent unsimplified equation
	$2500(x+20) - 2500x = 15x(x+20)$	<b>M1</b>	<b>FT</b> elimination of <i>their</i> fractions with algebraic denominators
	Correct simplification leading to $3x^2 + 60x - 10\,000 = 0$ AG	<b>A1</b>	
9(b)(iii)	48.59 and -68.59 <b>final answer</b>	3	<b>B1</b> for $\sqrt{60^2 - 4 \times 3 \times -10000}$ soi <b>B1</b> for $\frac{-60 \pm \sqrt{\text{their } 123600}}{2 \times 3}$
9(b)(iv)	36 minutes 27 seconds	3	<b>M2</b> for $\frac{2500}{\text{their } 48.59 + 20}$ or <b>M1</b> for $\frac{2500}{\text{their } 48.59}$
10(a)(i)	Triangle <i>B</i> at (2, -3), (3, -3), (3, -5)	2	<b>B1</b> for translation of correct triangle <i>B</i>
10(a)(ii)	Triangle <i>C</i> at (3, 3), (3, 9), (6, 3)	2	<b>B1</b> for two vertices correct or for $\begin{pmatrix} 3 & 0 \\ 0 & 3 \end{pmatrix} \begin{pmatrix} 1 & 2 & 1 \\ 1 & 1 & 3 \end{pmatrix}$ oe
10(a)(iii)	$\begin{pmatrix} \frac{1}{3} & 0 \\ 0 & \frac{1}{3} \end{pmatrix}$ oe	1	
10(a)(iv)	Enlargement Centre (3, -1.5) SF $-\frac{1}{3}$	3	<b>B1</b> for each
10(b)(i)	$\begin{pmatrix} 4 \\ 8 \end{pmatrix}$	2	<b>B1</b> for one component correct or <b>M1</b> for $2 \begin{pmatrix} 6 \\ 3 \end{pmatrix} - \begin{pmatrix} 8 \\ -2 \end{pmatrix}$ oe After 0 scored, <b>SC1</b> for answer $\begin{pmatrix} -4 \\ -8 \end{pmatrix}$
10(b)(ii)	$\begin{pmatrix} 9 \\ 0 \end{pmatrix}$	2	<b>B1</b> for one component correct or <b>M1</b> for $-\frac{3}{4}(\text{their } \overline{SR})$ or $\frac{1}{4}(\text{their } \overline{SR})$ soi

Question	Answer	Marks	Partial Marks
11(a)	$\angle ARB = \angle PRQ$ , [vertically] opposite $\angle RAB = \angle RQP$ , alternate [angles] $\angle RBA = \angle RPQ$ alternate [angles] $\triangle ARB$ and $\triangle QRP$ similar, equal angles	3	<b>B1</b> for one pair of angles stated with reason or for two pairs with no reasons or incorrect reasons  <b>B1</b> for a further correct pair of angles with reason
11(b)(i)	[AQ = ] 8.72 or 8.717[...]	2	<b>M1</b> for $\cos 55 = \frac{5}{AQ}$ or $\sin 35 = \frac{5}{AQ}$ oe
11(b)(ii)	[AR = ] 7.37[2...]	2	<b>M1</b> for $\cos 35 = \frac{AR}{9}$ or $\sin 55 = \frac{AR}{9}$ oe
11(b)(iii)	[Area $ARB =$ ] 18.8 to 19.2[...] or <b>FT</b> their $AR$	2	<b>M1</b> for $\frac{1}{2} \times \text{their } 7.37 \times 9 \times \sin 35$ oe Or $\frac{1}{2} \times \text{their } 7.37 \times \sqrt{9^2 - (\text{their } 7.37)^2}$
11(b)(iv)	19.6 to 19.7 <b>nfww</b> 	3	<b>M1</b> for $\tan 35 = \frac{PR}{\text{their } RQ}$ oe or $\frac{PR}{\text{their } RQ} = \frac{\text{their } RB}{\text{their } AR}$ oe where $\text{their } RQ = (\text{their } 8.72 - \text{their } 7.37)$  <b>M1</b> for their area $ARB + \frac{1}{2} \times \text{their } RQ \times \text{their } PR$