

Cambridge International A Level

MATHEMATICS
Paper 6 Probability & Statistics 2
MARK SCHEME
Maximum Mark: 50

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the October/November 2023 series for most Cambridge IGCSE, Cambridge International A and AS Level components, and some Cambridge O Level components.

Cambridge International A Level – Mark Scheme

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Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always whole marks (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

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Mathematics-Specific Marking Principles

- 1 Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.
- 2 Unless specified in the question, non-integer answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.
- 3 Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.
- 4 Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).
- Where a candidate has misread a number or sign in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 A or B mark for the misread.
- 6 Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

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Mark Scheme Notes

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

- Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- **B** Mark for a correct result or statement independent of method marks.
- DM or DB When a part of a question has two or more 'method' steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly, when there are several B marks allocated. The notation DM or DB is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
 - FT Implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only.
- A or B marks are given for correct work only (not for results obtained from incorrect working) unless follow through is allowed (see abbreviation FT above).
- For a numerical answer, allow the A or B mark if the answer is correct to 3 significant figures or would be correct to 3 significant figures if rounded (1 decimal place for angles in degrees).
- The total number of marks available for each question is shown at the bottom of the Marks column.
- Wrong or missing units in an answer should not result in loss of marks unless the guidance indicates otherwise.
- Square brackets [] around text or numbers show extra information not needed for the mark to be awarded.

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Abbreviations

AEF/OE Any Equivalent Form (of answer is equally acceptable) / Or Equivalent

AG Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)

CAO Correct Answer Only (emphasising that no 'follow through' from a previous error is allowed)

CWO Correct Working Only

ISW Ignore Subsequent Working

SOI Seen Or Implied

SC Special Case (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the

light of a particular circumstance)

WWW Without Wrong Working

AWRT Answer Which Rounds To

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Question	Answer	Marks	Guidance
1	$\frac{405 - 410}{\frac{20}{6}} \ [= -1.5]$	M1	For standardising, must have $\sqrt{36}$. Allow totals method $\frac{14580-14760}{\sqrt{14400}}$. No mixed methods.
	$\phi('-1.5') = 1 - \phi('1.5')$	M1	For area consistent with their working.
	= 0.0668	A1	
		3	

Question	Answer	Marks	Guidance
2	$\frac{134}{300} + z\sqrt{\frac{134}{300} \times \frac{166}{300}} = 0.487$	M1	For expression of the correct form.
	z = 1.405	A1	Accept 1.404, or anything that rounds to 1.39 to 1.41.
	$\phi^{-1}(1.405) = 0.9199 \text{ or } 0.92; 1 - 2(1 - 0.92)$	M1	Attempt area above or below their 1.405 and convert to a confidence level.
	$\alpha = 84$	A1	Allow $\alpha = 84\%$. cwo Note: final answer 0.84 scores A0.
		4	

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Question	Answer	Marks	Guidance
3(a)(i)	$\lambda = 3$	B1	For mean = 3.
	$1 - e^{-3}(1 + 3 + \frac{3^2}{2} + \frac{3^3}{3!}) \text{ or } 1 - e^{-3}(1 + 3 + 4.5 + 4.5)$ or $1 - (0.04979 + 0.14936 + 0.22404 + 0.22404)$	M1	Any λ . Allow one end error.
	= 0.353 (3 sf)	A1	No working scores B1.
		3	
3(a)(ii)	N(54, 54)	M1	soi
	$\frac{39.5 - 54}{\sqrt{54}} \ (= -1.973)$	M1	Allow with wrong or no continuity correction. For standardising with their mean and variance.
	$1 - \phi \ ('1.973')$	M1	For area consistent with their working.
	= 0.0242 (3 sf)	A1	Special case: if no working seen, 0.0242 scores SC B3 , 0.0284 scores SC B2 .
		4	
3(b)(i)	'Mean not constant' or' 'number of hits per minute not constant' or 'not a constant rate'	B1	
		1	
3(b)(ii)	$2p + p = 2 \times 0.3 \ [\Rightarrow p = 0.2]$ [where p is the rate per minute for night time]	M1	May be implied by answer.
	[During day-time]: Po(0.4). [During night-time]: Po(0.2)	A1	Accept Po(24) [per daytime hour], Po(12) [per night time hour]. Accept Po(288) [per day time shift], Po(144)[per night time shift]. Note: Po(432), Po(216) scores M0A0.
		2	

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Question	Answer	Marks	Guidance
4(a)	$E(A \text{ income}) = [10.3 \times 2.50] = 25.75 [\$]$	B1	Accept 3sf.
	$Var(A \text{ income}) = [5.76 \times 2.50^2] = 36 [\$^2]$	B1	
		2	
4(b)	$B \text{ income} \sim N(37.05, 101.506)$ or E(B income) = 37.05 and Var(B income) = 101.51	B1	Or N(37.1, 102) soi.
	A income – B income ~ N('25.75' – '37.05', '36' + '101.506')	M1	Ft their values for A and B.
	= N(-11.3, 137.506)	A1	Accept 3sf.
	$\frac{0 - (-'11.3')}{\sqrt{137.506'}} \ [= 0.964]$	M1	Standardising with their values from attempt at A income $-B$ income.
	$1 - \phi(0.964)$	M1	For area consistent with their values.
	= 0.168 or 0.167 (3 sf)	A1	cwo
		6	

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Question	Answer	Marks	Guidance
5	H ₀ : Population mean no. enquiries = 1.55 H ₁ : Population mean no. enquiries > 1.55	B1	Or "population mean no. enquiries = 0.31 (per minute)" oe. Allow ' λ = 1.55' or μ = '1.55'.
	$P(X \ge 5) = 1 - e^{-1.55} (1 + 1.55 + \frac{1.55^2}{2!} + \frac{1.55^3}{3!} + \frac{1.55^4}{4!})$ or $1 - e^{-1.55} (1 + 1.55 + 1.20125 + 0.62065 + 0.24050)$ or $1 - (0.21225 + 0.32898 + 0.25496 + 0.13173 + 0.05105)$	M1	Allow one end error, e.g. extra term: $e^{-1.55} \times \frac{1.55^5}{5!}$.
	= 0.0210 (3 sf)	A1	Allow 0.021. SC B1 no working scores B1 instead of M1A1.
	0.0210 < 0.025	M1	For valid comparison.
	[Reject H_0] There is sufficient evidence [at 2.5% level] to suggest that mean no. of enquiries has increased.	A1 FT	In context, not definite, e.g., not "Mean no. of enquiries has increased". No contradictions.
		5	Note: $e^{-1.55} \times \frac{1.55^5}{5!} = 0.0158 < 0.025$: scores max B1

Question	Answer	Marks	Guidance
6(a)	$p + \frac{13}{10}p \le \frac{1}{2} \implies p \le \frac{5}{23} \text{ AG}$	B1	Allow '=' in working but need an inequality in the answer. Allow $0 .$
		1	

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Question		Answer				Marks	Guidance
6(b)	e.g.	0.5 - 2.3p, 0 to a 2p + 2.6p, $2 \times (a \text{ to } 3)$	p + 1.3p, a to 3 0.5 - 1.3p, 0 to b	$2 \times 1.3p$, $2 \times (b \text{ to } 3)$ 0.5 + 1.3p, b to 6	2.3p + 1.3p, $a to 3 + b to 3$	M1	Any correct expression for the probability of a relevant region.
	$\frac{18}{5}p$	or 3.6 <i>p</i>				A1	
						2	

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Question	Answer	Marks	Guidance
6(c)	$\frac{1}{36} \int_{a}^{2} (6x - x^{2}) \mathrm{d}x = \frac{5}{27}$	M1	Attempt to integrate with correct limits and equate to $\frac{5}{27}$, oe. Integrate from 2 to $6-a$ and equate $\frac{18}{5}p = \frac{2}{3}$. Integrate from a to 3 and equate to $\frac{23}{54}$. Integrate from 0 to a and equate to $\frac{2}{27}$.
	$\left[\Rightarrow \frac{1}{36} \left[3x^2 - \frac{x^3}{3} \right]_a^2 = \frac{5}{27} \Rightarrow \frac{1}{36} \left(12 - \frac{8}{3} - 3a^2 + \frac{a^3}{3} \right) = \frac{5}{27} \right]$	M1	For integrating and substitution of limits to form cubic in <i>a</i> .
	$a^3 - 9a^2 + 8 = 0$	A1	Any correct three term cubic equation in <i>a</i> .
	$(a-1)(a^2-8a-8)=0$	M1	Attempt to factorise their cubic equation.
	$a = \frac{8 \pm \sqrt{96}}{2} = 4 \pm \sqrt{24}$ or -0.899 or 8.90, [not between 0 and 6]		
	a = 1 only [other two values rejected]	A1	SC B1 for $a = 1$ only, if no method seen for solving the cubic.
		5	

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Question	Answer	Marks	Guidance
7(a)	Est $(\mu) = 23/50 = 0.46$	B1	
	Est $(\sigma) = \sqrt{\frac{50}{49}} \times \sqrt{\frac{13.02}{50} - 0.46^2}$ or Est $(\sigma^2) = \frac{50}{49} \times \left(\frac{13.02}{50} - 0.46^2\right)$ oe	M1	For an expression of the correct form for unbiased standard deviation or variance.
	Or estimated unbiased variance = $\frac{1}{49} \left(13.02 - \frac{(23.0)^2}{50} \right)$		
	Est $(\sigma) = 0.22315$ or Est $(\sigma^2) = 0.0497959 = \left(\frac{61}{1225}\right)$ or 0.0498	A1	
	$\frac{0.46 - 0.5}{\frac{0.22315'}{\sqrt{50}}}$	M1	Standardising with their values.
	=-1.268 or -1.267 or =-1.27 (3sf)	A1	
	-1.268 > -1.645 or 0.102 to $0.103 > 0.05$	M1	For a valid comparison.
	[Do not reject Ho] There is insufficient evidence [at 5% level] that the mean concentration is less than 0.5.	A1 FT	In context, not definite. E.g., not 'Mean concentration is not less than 0.5'. No contradictions.
		7	

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Question	Answer	Marks	Guidance
7(b)	$\frac{\text{cv} - 0.5}{\frac{0.22315}{\sqrt{50}}} = -1.645$	M1	
	cv = 0.448(1) or 0.448 (3 sf)	A1	
	$\frac{0.448' - 0.4}{\frac{0.22315'}{\sqrt{50}}} $ [=1.521 to 1.524]	M1	
	$1 - \phi(1.524)$	M1	For area consistent with their working.
	= 0.0638 to 0.0642	A1	
		5	

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